

Calc 3 HW 3

Note Time

9/8/2011

- ① If $\vec{r} = \langle x, y, z \rangle$ and $\vec{r}_0 = \langle x_0, y_0, z_0 \rangle$,

describe the set of all points (x, y, z) such

that

$$\|\vec{r} - \vec{r}_0\| = 1$$

- ② Which expression makes sense; where \cdot is dot-product

- a) $(\vec{a} \cdot \vec{b}) \vec{c}$
- b) $\|\vec{a}\| (\vec{b} \cdot \vec{c})$
- c) $\vec{a} \cdot (\vec{b} + \vec{c})$
- d) $\vec{a} \cdot \vec{b} + \vec{c}$
- e) $\|\vec{a}\| \cdot (\vec{b} + \vec{c})$

- ③ Find dot product of two vectors if their lengths

are 6 and $\frac{1}{3}$ and the angle between them is $\pi/4$.

- ④ Find $\vec{a} \cdot \vec{b}$ for

- a) $\vec{a} = \langle -2, \frac{1}{3} \rangle, \vec{b} = \langle -5, \pi \rangle$
- b) $\vec{a} = \langle 4, 1, \frac{1}{4} \rangle, \vec{b} = \langle 6, -3, -8 \rangle$

- ⑤ Find angle between \vec{a} and \vec{b} for:

- a) $\vec{a} = \langle \sqrt{3}, 1 \rangle, \vec{b} = \langle 0, 5 \rangle$
- b) $\vec{a} = \langle 4, 0, 2 \rangle, \vec{b} = \langle 2, -1, 0 \rangle$
- c) $\vec{a} = i + 2j - 2k, \vec{b} = 4i - 3k$

- ⑥ Are the vectors orthogonal, parallel, or neither?

- a) $\vec{a} = \langle -5, 3, 7 \rangle, \vec{b} = \langle 6, -8, 2 \rangle$

- b) $\vec{a} = \langle -3, 9, 6 \rangle, \vec{b} = \langle 4, -12, -8 \rangle$

- c) $\vec{a} = \langle 7, 0, -2 \rangle, \vec{b} = \langle 2, 5, 7 \rangle$

⑦ For what values of b are the vectors $\langle -6, b, 2 \rangle$ and $\langle b, b^2, b \rangle$ orthogonal?

⑧ Find the directional angles (cosines) of $\langle 3, 4, 5 \rangle$

⑨ Find the angle between a diagonal of a cube and one of its edges.