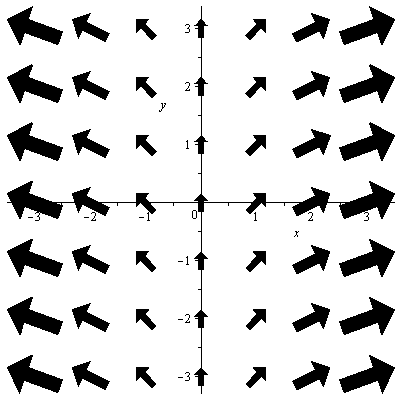
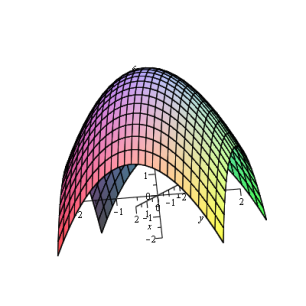
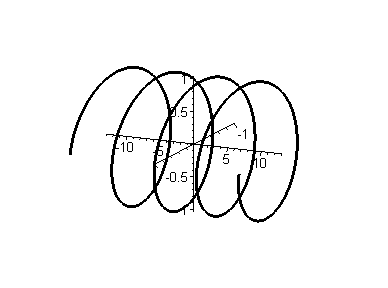
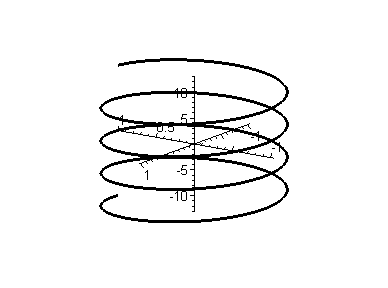
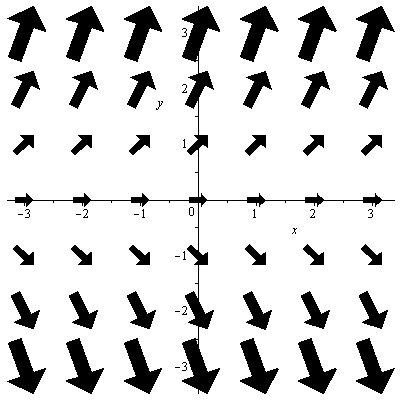
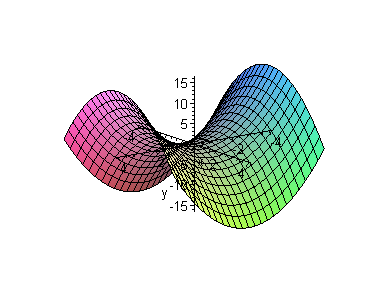
**Calc 3 – Final Exam**

This is a take-home, open-book, open notes exam; you even may use Maple or Wolfram Alpha to assist you in calculations. You must, however, complete it *entirely on your own*. It is due on the day of our final exam – no exception. Please indicate clearly where each problem starts and do not forget to put your name on your exam.

1. Please state the following:
2. an equation relating the dot product of two vectors with the angle between them
3. the definition of the gradient of a function and its properties
4. the main difference between Green’s and Stoke’s Theorem as far as the vector field is concerned
5. the Divergence Theorem (also known as Gauss’ Theorem)

2. Match the following pictures with the algebraic expressions below.

[A]  [B]  [C]

[D]  [E]  [F] 

(1)  (2)  (3) 

(4)  (5)  (6) 

3. Determine if the plane through the points , , and is perpendicular to the plane given by the equation. Then find the distance of the second plane to the point (6,2,-1)

4. A baseball is hit 4 feet above ground at an initial velocity of feet per second. Find the maximum height reached by the baseball. Will it clear a 15-foot high fence located 350 feet from home base?

5. Determine the following limits, if possible, or explain why they don’t exist.

# 6. Find all critical points and test them for relative extrema for the function (*Hint: There are two critical points*)

7. Suppose . Find (**a**) , i.e. the gradient of *f* (**b**) at , i.e. the directional derivative of *f* in the direction of *u*, where and (**c**) a unit vector in the direction of maximal increase of *f* if you are currently standing at *P(1,0).*

8. Evaluate the following integrals:

1. , where *R* is the triangular region bounded by *y = 0*, *y = x*, and *x = 1*
2. , where *C* is the curve given by for
3. , where and *C* is the line segment from to
4. The flux of the vector field , where S is the portion of the surface between the coordinate planes.

# 9. For the following integrals there could be more than one way to evaluate them. Use the most convenient method and quote the appropriate theorem, if necessary.

1.  where  and C a curve from (1,0,1) to (1,4,4)
2.  where  and *C* is the closed curve given by the boundary of the square with corner points (-1,-1), (-1,1), (1, -1), and (1,1).
3.  where *C* is the closed curve given by the boundary of the triangle with corner points (0,0), (0,1), and (1, 0), oriented counter-clockwise.
4.  where  and *S* is given by 
5.  where  and C is the boundary of the surface *S* given by , restricted by the coordinate planes and oriented counter-clockwise.

**EXTRA**. Find the sign (pos, neg, zero) of each expression (assume the vector field is 3D). Explain!

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