

① How many n -th order partial derivatives does a function $f(x, y)$ have? How about a function $f(x, y, z)$?

② Find all 2nd-order partial derivatives of:

a) $f(x, y) = x^3 y^5 + 2x^4 y$

b) $f(x, y) = x e^{xy}$

c) Verify that $f_{xy} = f_{yx}$ in the above examples.

③ Find the given partial derivative:

a) $f(x, y, z) = xy^2 z^3$; f_{xyz}

b) $f(x, y) = \sin(xy)$; f_{xy}

c) $f(x, y) = x^4 + x^2 y^2 + 5xy^3$; f_{xxyyxx}