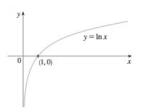
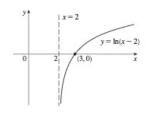
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158 - CHAPTER 3 INVERSE FUNCTIONS





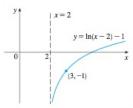


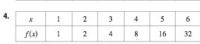
FIGURE 16

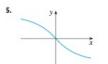
3.2 **EXERCISES**

- I. (a) What is a one-to-one function?
 - (b) How can you tell from the graph of a function whether it is one-to-one?
- 2. (a) Suppose f is a one-to-one function with domain A and range B. How is the inverse function f^{-1} defined? What is the domain of f^{-1} ? What is the range of f^{-1} ?
 - (b) If you are given a formula for f, how do you find a formula for f^{-1} ?
 - (c) If you are given the graph of f, how do you find the graph of f^{-1} ?

3-14 • A function is given by a table of values, a graph, a formula, or a verbal description. Determine whether it is one-to-one.

3.	x	1	2	3	4	5	6
	f(x)	1.5	2.0	3.6	5.3	2.8	2.0











9.
$$f(x) = x^2 - 2x$$

10.
$$f(x) = 10 - 3x$$

- 11. g(x) = 1/x
- 12. $g(x) = \cos x$
- 13. f(t) is the height of a football t seconds after kickoff.
- 14. f(t) is your height at age t.
- . . .
- 15. If f is a one-to-one function such that f(2) = 9, what is $f^{-1}(9)$?
- 16. If $f(x) = x + \cos x$, find $f^{-1}(1)$.
- 17. If $g(x) = 3 + x + e^x$, find $g^{-1}(4)$.
- 18. The graph of f is given.

 - (a) Why is f one-to-one?
 (b) What are the domain and range of f⁻¹?
 - (c) What is the value of f⁻¹(2)?
 - (d) Estimate the value of f⁻¹(0).



- 19. The formula $C = \frac{5}{9}(F 32)$, where $F \ge -459.67$, expresses the Celsius temperature C as a function of the Fahrenheit temperature F. Find a formula for the inverse function and interpret it. What is the domain of the inverse function?
- 20. In the theory of relativity, the mass of a particle with speed v is

$$m = f(v) = \frac{m_0}{\sqrt{1 - v^2/c^2}}$$

where m_0 is the rest mass of the particle and c is the speed of light in a vacuum. Find the inverse function of f and explain its meaning.

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21-26 • Find a formula for the inverse of the function.

21. $f(x) = \sqrt{10 - 3x}$

2x + 3

23. $f(x) = e^{x^3}$

24. $y = 2x^3 + 3$

25. $y = \ln(x + 3)$

27-28 • Find an explicit formula for f⁻¹ and use it to graph f^{-1} , f, and the line y = x on the same screen. To check your work, see whether the graphs of f and f^{-1} are reflections about the line.

27. $f(x) = x^4 + 1$, $x \ge 0$ **28.** $f(x) = 2 - e^x$

29-30 • Use the given graph of f to sketch the graph of f^{-1} .





31-34

- (a) Show that f is one-to-one.
- (b) Use Theorem 7 to find $(f^{-1})'(a)$.
- (c) Calculate f⁻¹(x) and state the domain and range of f⁻¹.
- (d) Calculate (f-1)'(a) from the formula in part (c) and check that it agrees with the result of part (b).
- (e) Sketch the graphs of f and f⁻¹ on the same axes.
- **31.** $f(x) = x^3$, a = 8
- **32.** $f(x) = \sqrt{x-2}$, a = 2
- **33.** $f(x) = 9 x^2$, $0 \le x \le 3$, a = 8
- **34.** f(x) = 1/(x-1), x > 1, a = 2

35-38 • Find (f⁻¹)'(a).

- **35.** $f(x) = x^3 + x + 1$, a = 1
- **36.** $f(x) = x^5 x^3 + 2x$, a = 2
- 37. $f(x) = 3 + x^2 + \tan(\pi x/2), -1 < x < 1, a = 3$
- **38.** $f(x) = \sqrt{x^3 + x^2 + x + 1}$, a = 2
- 39. Suppose f^{-1} is the inverse function of a differentiable function f and f(4) = 5, $f'(4) = \frac{2}{3}$. Find $(f^{-1})'(5)$.
- 40. Suppose f^{-1} is the inverse function of a differentiable function f and let $G(x) = 1/f^{-1}(x)$. If f(3) = 2 and $f'(3) = \frac{1}{9}$, find G'(2).

SECTION 3.2 INVERSE FUNCTIONS AND LOGARITHMS . 159

- 41. (a) How is the logarithmic function $y = \log_a x$ defined?
 - (b) What is the domain of this function?
 - (c) What is the range of this function?
 - (d) Sketch the general shape of the graph of the function $y = \log_a x \text{ if } a > 1.$
- 42. (a) What is the natural logarithm?
 - (b) What is the common logarithm?
 - (c) Sketch the graphs of the natural logarithm function and the natural exponential function with a common set of
- 43-46 Find the exact value of each expression (without a calculator).
- 43. (a) log₂64
- (b) log₆ ½
- 44. (a) log₈2
- (b) $\ln e^{\sqrt{2}}$
- 45. (a) log₁₀ 1.25 + log₁₀ 80 (b) $\log_5 10 + \log_5 20 - 3 \log_5 2$
- 46. (a) 2^(log₂3 + log₂5)
- (b) e3ln2

47-50 . Use the properties of logarithms to expand the

- 47. $\log_2\left(\frac{x^3y}{z^2}\right)$
- 48. $\ln \sqrt{a(b^2+c^2)}$
- 49. ln(uv)
- 51-53 Express the given quantity as a single logarithm.
- 51. 2 ln 4 ln 2
- 52. $\ln x + a \ln y b \ln z$
- **53.** $\ln(1+x^2) + \frac{1}{2} \ln x \ln \sin x$
- 54. Use Formula 14 to evaluate each logarithm correct to six decimal places.
 - (a) log₁₂ 10
- (b) log₂ 8.4
- 55-56 Use Formula 14 to graph the given functions on a common screen. How are these graphs related?
- **55.** $y = \log_{1.5} x$, $y = \ln x$, $y = \log_{10} x$, $y = \log_{50} x$
- **56.** $y = \ln x$, $y = \log_{10} x$, $y = e^x$, $y = 10^x$
-
- 57. Suppose that the graph of $y = \log_2 x$ is drawn on a coordinate grid where the unit of measurement is an inch. How many miles to the right of the origin do we have to move before the height of the curve reaches 3 ft?
- $f(x) = x^{0.1}$ and $g(x) = \ln x$ by graphing both f and g in several viewing rectangles. When does the graph of f finally surpass the graph of g?

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