RSA Cryptography.

1. This question will do a simple RSA encoding and decoding. Assume that the letters of the alphabet correspond to the numbers 1-26. ( $A=1, B=2, \ldots, Z=26$; only capital letters are used).
a. If $\boldsymbol{p}=\mathbf{7}$ and $\boldsymbol{q}=\mathbf{1 3}$, what is $\boldsymbol{n}$ and what are the three smallest possible numbers for $\boldsymbol{e}$ ?
b. If $\boldsymbol{p}=7, \boldsymbol{q}=\mathbf{1 3}$, and $\boldsymbol{e}=\mathbf{7}$, what is $\boldsymbol{d}$ (the multiplicative inverse of $\boldsymbol{e}$ )?
c. Use ( $\mathbf{d}, \mathbf{n}$ ) to decrypt the following message, encrypted with the private key $(\mathbf{e}, \mathbf{n})$ :

35014846016701216950332550704473504474657471347333318447
2. Create your very own private and public key-pairs $(e, n)$ and ( $d, n$ ). You cannot use any of the $n$ 's we used as examples in class. Send me an email containing your public key. I will use it to encode a secret message just for you. Decode that message and send it back to me in clear text.

