

## Calc I - Assignment # 19

- ① Estimate the volume below  $z = xy$  and above the rectangle  $D = [0, 6] \times [0, 4]$  by dividing the  $x$ -interval into 4 parts, the  $y$ -interval into 3 parts, and taking as height the value of  $f(x, y)$  at each upper-right corner. Compare your answer

with

$$\iint_D xy \, dA$$

- ② Evaluate  $\iint_R 5 - x \, dA$ ,  $R = [0, 5] \times [0, 3]$

Both algebraically and geometrically.

- ③ Use Fubini's Theorem to compute:

a)  $\int_0^3 \int_0^1 (1 + 4xy) \, dx \, dy$

b)  $\int_0^1 \int_1^2 (4x^3 - 9x^2y^2) \, dy \, dx$

c)  $\int_0^1 \int_0^1 xy \sqrt{x^2 + y^2} \, dy \, dx$

d)  $\int_0^1 \int_0^1 \sqrt{s+t} \, ds \, dt$

$$c) \iint_R \frac{1+x^2}{1+y^2} dA, \quad R = [0,1] \times [0,1]$$

$$c) \iint_R \frac{x}{x^2+y^2} dA, \quad R = [1,2] \times [0,1]$$

④ Find the volume under  $z = 4 + x^2 - y^2$  and above  $R = [-1,1] \times [0,2]$

⑤ Find the volume of the solid enclosed by  $z = (1 + e^x \sin(y))$  and the planes  $x = \pm 1$ ,  $y = 0$ ,  $y = \pi$ , and  $z = 0$ .

⑥ Read Fubini's Theorem carefully. Then use Maple to compute

$$\int_0^1 \int_0^1 \frac{x-y}{(x+y)^3} dy dx \quad \text{and}$$

$$\int_0^1 \int_0^1 \frac{x-y}{(x+y)^3} dx dy.$$

Explain.