

## Calc 3 HW: Planes + Intersections

① Find the scalar equation for the following planes

a) Through  $P(-1, 0, 1)$ ,  $Q(2, 3, 1)$ ,  $R(1, 1, 0)$

b) Through origin and parallel to  $x+y+z=15$

c) Through point  $P(-2, 1, -1)$  and containing the line  $\ell(t) = \langle 1, 3, -2 \rangle + t \langle 3, 2, 1 \rangle$

② Is  $P(0, 3, -2)$  on the plane  $5x + 6y + 9z = 0$ ? How about  $\ell(t) = \langle 1, 3, -2 \rangle + t \langle 4, 1, 1 \rangle$ ?

③ Find the point of intersection of the lines

$\ell_1(t) = \langle 1, 1, 0 \rangle + t \langle 1, -1, 2 \rangle$  and  $\ell_2(t) = \langle 2, 0, 2 \rangle + s \langle -1, 1, 0 \rangle$

Then find the equation of the plane containing both lines.

④ Which of these planes are parallel:

$$\text{plane}_1: 4x - 2y + 6z = 3 \quad \text{plane}_2: 4x - 2y - 2z = 6$$

$$\text{plane}_3: -6x + 3y - 9z = 5 \quad \text{plane}_4: z = 2x - y - 9$$

⑤ Where does the line through  $(1, 0, 1)$  and  $(4, -2, 2)$  intersect the plane  $x + y + z = 6$ ?

⑥ Find equation of a plane with  $x$ -intercept A,  $y$ -intercept B, and  $z$ -intercept C.

⑦ Equation of line through  $(1, 0, 6)$  and perpendicular to the plane  $x + 3y + z = 5$

⑧ Find line of intersection between planes

$$x + y + z = 1 \quad \text{and} \quad x - 2y + 3z = 1$$