

Calc 3: Assignment

Note Title

11/9/2011

① Sketch the following vector fields

a) $\vec{F}(x,y) = \langle 1, x \rangle$

b) $\vec{F}(x,y) = \langle y, \frac{1}{2} \rangle$

c) $\vec{F}(x,y) = \frac{1}{\sqrt{x^2+y^2}} \langle y, x \rangle$

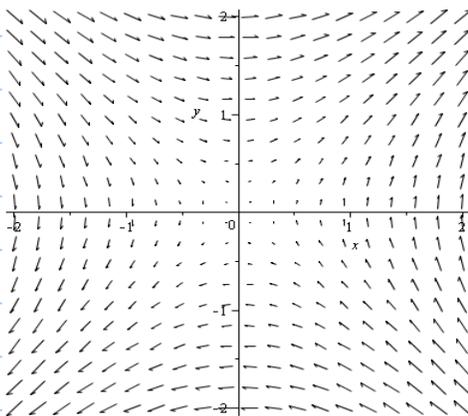
② Match the vector fields with the plots.

a) $F(x,y) = \langle y, \frac{1}{x} \rangle$

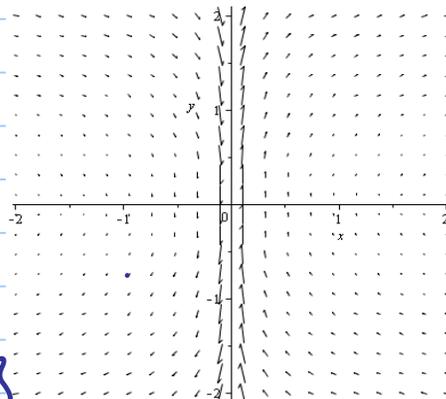
b) $F(x,y) = \langle x-2, x+1 \rangle$

c) $F(x,y) = \langle y, x \rangle$

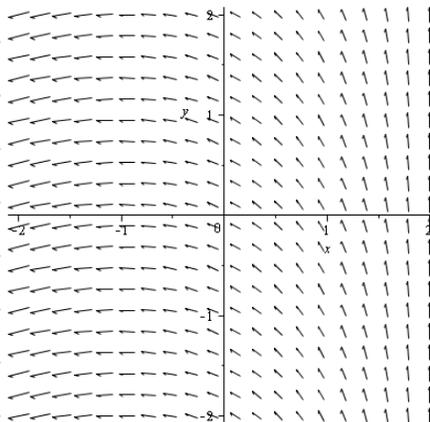
d) $F(x,y) = \langle 1, \sin(y) \rangle$



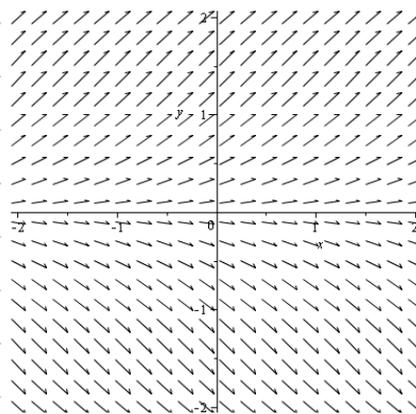
A



B



C



D

④ Use Maple to plot $F(x,y) = \langle y^2 - 2xy, 3xy - 6x^2 \rangle$

⑤ Recall that if $\vec{F} = \langle M, N \rangle$ is conservative, then $\frac{\partial N}{\partial x} = \frac{\partial M}{\partial y}$. Which vector fields are conservative:

a) $\vec{F} = \langle 2x - 3y, -3x + 4y - 9 \rangle$

b) $\vec{F} = \langle e^x \cos(y), e^x \sin(y) \rangle$

c) $\vec{F} = \langle 3x^2 + 2y^2, 4xy + 3 \rangle$

⑥ For the vector fields in ⑤ that are conservative, find the potential function

⑦ Find the curl (F) and div (F) for:

a) $\vec{F} = \langle xyz, 0, -x^2y \rangle$

b) $\vec{F} = \langle x^2yz, xy^2z, xyz^2 \rangle$

c) $\vec{F} = \langle e^x, e^{xy}, e^{xy^2} \rangle$

⑧ Which of these vector fields is conservative:

a) $\vec{F} = \langle y^2z^3, 2xyz^3, 3xy^2z^2 \rangle$

b) $\vec{F} = \langle e^z, 1, xe^z \rangle$

c) $\vec{F} = \langle y \cos(xy), x \cos(xy), -\sin(z) \rangle$

d) $\vec{F} = \langle 2x^2 - 3x^2y^2z, 3x^2y^2 - 2x^3y + x \rangle$

If it is conservative, find potential function.

⑧ If $f: \mathbb{R}^3 \rightarrow \mathbb{R}$ is a function and $\vec{F}: \mathbb{R}^3 \rightarrow \mathbb{R}^3$ is a vector field, which expression is meaningful:

$$\text{curl}(f)$$

$$\text{grad}(f)$$

$$\text{div}(\vec{F})$$

$$\text{curl}(\text{grad}(f))$$

$$\text{grad}(\vec{F})$$

$$\text{grad}(\text{div}(\vec{F}))$$

$$\text{div}(\text{grad}(f))$$

$$\text{grad}(\text{div}(f))$$

$$\text{curl}(\text{curl}(\vec{F}))$$

$$\text{div}(\text{div}(\vec{F}))$$

$$(\text{grad}(f)) \times (\text{div}(\vec{F}))$$

$$\text{div}(\text{curl}(\text{grad}(f)))$$