

Calc I - Assignment 6

Note Title

9/14/2011

① Find area of parallelogram with vertices

$A(-2,1)$, $B(0,4)$, $C(4,2)$, and $D(2,-1)$. Hint: to

take cross products of \mathbb{R}^2 vectors, consider them embedded in \mathbb{R}^3 with z -coordinates 0.

② Let P be a point not on the line L that

passes through Q and R . Show that the

distance d from P to L is

$$d = \frac{\|\vec{a} \times \vec{b}\|}{\|\vec{a}\|}$$

where $\vec{a} = \vec{QR}$ and $\vec{b} = \vec{QP}$. Use that

formula to find the distance of $P(1,1,1)$ to

the line through $Q(0,6,9)$ and $R(-1,4,7)$

③ Find the parametric equation of the lines

a) through $(6,-5,2)$ parallel to $3i+2j-k$

b) through $(1,2,3)$ and $(-4,3,0)$

c) through $(1,9,6)$ perpendicular to the

$$\text{plane } x+3y+z=5$$

d) through $(2,1,0)$, perpendicular to both $i+j$

and $j+k$

④ Are the following lines parallel, skew, or intersecting. If they intersect, find that point.

a) $L_1: \langle -6t, (1+9t), -3t \rangle$

$L_2: \langle 1+2s, 4-3s, s \rangle$ —

b) $L_1: \langle 1+2t, 3t, 2-t \rangle$

$L_2: \langle -1+s, 4+s, 1+3s \rangle$

⑤ Find an equation of the plane:

a) through $(6, 3, 2)$ perpendicular to $\langle -2, 1, 5 \rangle$

b) through $(-1, 6, -5)$ parallel to $x+y+z=0$

c) through $(3, -1, 2)$, $(8, 2, 4)$, and $(-1, -2, -3)$

d) through $(6, 0, -2)$ containing the line

$$l(t) = (4, 3, 7) + t \langle -2, 5, 4 \rangle$$

⑥ Find the cosine of the angle between the planes $x+y+z=0$ and $x+2y+3z=1$

⑦ Sketch the following planes

a) $2x + 5y + z = 10$

b) $3x + y + 2z = 6$