

Quiz

1. Answer the following questions **and** provide a reason for your answer:
 - a) Can you apply the Fundamental Theorem of line integrals to the function $f(x, y, z) = xy \sin(z) \cos(x^2 + y^2)$?
 - b) Can you apply the Fundamental Theorem of line integrals to the vector field $\vec{F}(x, y) = \langle 6xy^2 - 3x^2, 6x^2y + 3y^2 - 2x^3 \rangle$?
 - c) Can you apply Green's theorem to a curve C, which is a straight line from (0,0,0) to (1,2,3)?

2. Evaluate the following integrals, using whatever method/shortcut you think is most appropriate (including Maple):
 - a) $\int_C \vec{F} \cdot d\vec{r}$ where $\vec{F}(x, y) = \langle y, x^2 \rangle$ and C is the curve given by $\vec{r}(t) = \langle 4 - t, 4t - t^2 \rangle$, $0 \leq t \leq 3$

 - b) $\int_C \vec{F} \cdot d\vec{r}$ where $\vec{F}(x, y) = \langle e^x \cos(y), -e^x \sin(y) \rangle$ and C is the curve $\vec{r}(t) = \langle 2 \cos(t), 2 \sin(t) \rangle$, $0 \leq t \leq 2\pi$

 - c) $\int_C 2xyz dx + x^2 z dy + x^2 y dz$ where C is some smooth curve from (0,0,0) to (1,4,3)

 - d) $\int_C y^3 dx + (x^3 + 3xy^2) dy$ where C is the path from (0,0) to (1,1) along the graph of $y = x^3$ and from (1,1) back to (0,0) along the graph of $y = x$.

 - e) $\int_C y dx + 2x dy$ where C is the boundary of the square with vertices (0,0), (0,2), (2,0), and (2,2)