

7. Recall that using the method of Partial Fraction Decomposition can be used to convert a rational function  $\frac{p(x)}{q(x)}$  into a sum of simpler functions, each of which can easily be integrated.

a. Given that  $\frac{x-1}{x^2+x-12} = \frac{A}{x+4} + \frac{B}{x-3}$ , find the value of the constants  $A$  and  $B$

b. Given that  $\frac{x}{(x+2)(x-1)^2} = -\frac{2}{9(x+2)} + \frac{2}{9(x-1)} + \frac{1}{3(x-1)^2}$ , compute  $\int \frac{x}{(x+2)(x-1)^2} dx$

8. Integrate using any method:

a)  $\int_0^1 x^3 e^{x^4} dx$

b)  $\int \frac{1}{x\sqrt{1-x^2}} dx$  (you could use  $\int \sec(x) dx = \ln(\sec(x) + \tan(x))$  or  $\int \csc(x) dx = \ln(\csc(x) - \cot(x))$ )

c)  $\int x \sin(x) dx$

d)  $\int \cos^2(x) \sin^3(x) dx$

e)  $\int_0^{\infty} \frac{2x}{(x^2 + 5)^2} dx$

f)  $\int_{-2}^2 \frac{1}{(x+1)^2} dx$

9. Please find the following limits (you might find l'Hospital's rule helpful for *some* limits)

a)  $\lim_{x \rightarrow 0} \frac{\sin(x)}{1+x}$

b)  $\lim_{x \rightarrow 1} \frac{1-x+\ln(x)}{1-\sin(\frac{\pi}{2}x)}$

c)  $\lim_{x \rightarrow \infty} \frac{x^2-3x+2}{2-x^2}$

d)  $\lim_{x \rightarrow 0^+} x \ln(x)$

EXTRA CREDIT: Find  $\int \arctan(x) dx$