

Panel 1

Summary

Compound interest: $S = P(1+r)^n$

Effective rate: $r_e = (1 + \frac{r}{n})^n - 1$

Present Value: $= PV(\text{rate}, \text{aper}, \text{pmt}, \text{fv})$

Future Value: $= FV(\text{rate}, \text{aper}, \text{pmt}, \text{pv})$

Payments: $= PMT(\text{rate}, \text{aper}, \text{pv})$

1

Panel 2

① You sign for a loan with payments of $\$200$ per month at 10% over 10 years compounded monthly. (PV)

② You want to setup a trust fund of $\$50,000$ in 15 years at 3% interest compounded monthly with monthly payments of $\$150,-$. (PV)

③ You invest $\$150$ per month at 7% compounded monthly for 4 years. How much will you have? (FV)

④ You take out a loan for $\$20,000$ over 5 years at 4% interest compounded monthly. Payments per month? (PMT)

Panel 3

- ① You sign for a loan with payments of \$200 per month at 10% over 10 years compounded monthly. How much money do you get?

$$= PV\left(\frac{0.1}{12}, 120, -200\right) = \underline{15134}$$

Guess: $200 \times 120 = \underline{24000}$

3

Panel 4

- ② You want to setup a trust fund of \$50,000 in 15 years at 3% interest compounded monthly with monthly payments of \$150. What's the principle to pay initially?

Ball-park: $150 \times 15 \times 12 = \underline{27000}$, so invest $\approx \underline{23000}$

$$= PV\left(\frac{0.03}{12}, 12 \times 15, -150, 50000\right) = \underline{\underline{\$10179}}$$

4

Panel 5

③ You invest \$150 per month at 7% compounded monthly for 4 years. How much will you have?

$$= FV \left(\frac{0.07}{12}, 4 \cdot 12, -150 \right) = 9291$$

Guess: $150 \times 4 \times 12 = \underline{\underline{7200}}$

5

Panel 6

④ You take out a loan for \$20,000 over 5 years at 4% interest compounded monthly. Payments per month?

Guess: $\frac{20000}{60} = \$333.33$

$$= PMT \left(\frac{0.04}{12}, 60, -20000 \right) = \underline{\underline{\$369.33}}$$

$$369.33 \times 60 = \underline{\underline{22099.80}}$$

6

Panel 7

Last question: Suppose you want to purchase a house. You need a loan of \$200,000 over 30 years. Bank A offers 5%, Bank B offers 4.7%. What is the savings over the life of the loan if you make monthly payments and monthly compounding.

$$A: = \text{PMT} \left(\frac{0.05}{12}, 30 \times 12, -200000 \right) = \$1073.64$$

$$\text{total amount bank A gets in } \$1073.64 \times 30 \times 12 = \underline{\underline{\$386510.40}}$$

$$B: = \text{PMT} \left(\frac{0.047}{12}, 30 \times 12, -200000 \right) = \$1037.64$$

$$\text{in total: } \$1037.64 \times 30 \times 12 = \underline{\underline{\$373320}}$$

↑
↓ difference is
~13000

7

Panel 8

7. Suppose you invest \$250 at a nominal interest rate of 7% compounded quarterly.
- What is the *effective* rate of interest?
 - How much is your investment worth after 5 years?
 - How would you use the *effective* rate to compute the answer for part (b)

$$a) r_e = \left(1 + \frac{r}{n} \right)^n - 1 = \left(1 + \frac{0.07}{4} \right)^4 - 1 = 0.0718 \text{ or } \underline{\underline{7.18\%}}$$

$$b) S = 250 \left(1 + \frac{0.07}{4} \right)^{4 \cdot 5} = \underline{\underline{\$353.69}}$$

$$c) S = 250 \left(1 + \frac{0.0718}{1} \right)^5 = \underline{\underline{\$353.59}}$$

\$1000 over 1 year

8

Panel 9

8. Suppose \$8,000 is invested in an account. How much money is in the account in 6 years if the interest rate is 5% compounded: a) monthly b) continuously?

$$a) S = 8000 \left(1 + \frac{0.05}{12}\right)^{72} = \underline{10792.}$$

Recall: $\lim_{n \rightarrow \infty} \left(1 + \frac{r}{n}\right)^n = e$ $\left(1 + \frac{r}{n}\right)^{nt}$ new!

Continuous Compound Interest is: $S = P e^{rt}$, $r = \text{rate}$, $t = \# \text{ years}$

$$b) S = 8000 e^{0.05 \cdot 6} = \underline{10798.84}$$

9

Panel 10

WolframAlpha

integrate $2x^2 / (5-x^3)$

Indefinite integral:

$$\int \frac{2x^2}{5-x^3} dx = -\frac{2}{3} \log(x^3 - 5) + \text{constant}$$

WolframAlpha

integrate $32x^2 / (5-x)^4$ for x from 0 to 1

Definite integral:

$$\int_0^1 \frac{32x^2}{(5-x)^4} dx = \frac{1}{30} \approx 0.0333333$$

Talk on Copy right!
 Richard Skellern
 April 19, 2:30-4:30
 JH Auditorium

10