

Panel 1

Contingency Tables
Do Males/Females vote differently.

	Male	Female	
Demos	4 $\frac{4}{12}$ $\frac{4}{12}$	3 $\frac{3}{13}$	7
Ind.	4 40% $\frac{4}{12}$	6 60%	10
Repub.	4 $\frac{4}{12}$	2 $\frac{6}{13}$ $\frac{2}{13}$	6
Others	$\frac{2}{11}$ = 0.18%	2	2
	12	13	25

How many of the Demos are male? $\frac{4}{7}$ (Row %)
How many women are indep. $\frac{6}{13}$ (Col %)

Panel 2

What is the point of the expected values?
They are those counts that are to be expected if two variables have nothing to do with each other, i.e. if there is no relation between them.

2 Tables: actual counts:

#	#
#	#

 what is actually the case

expected counts:

#	#
#	#

 what are expected

Ex:

10	20
25	10

 actual

11	19
24	11

 expected \Rightarrow No Relation

Panel 3

10	20
25	10

actual

5	33
6	19

expected

→ Related

In other words, you compute

$$\chi^2 = \sum \left(\frac{\text{difference between actual and expected counts}}{\text{expected count}} \right)^2$$

If sum is large \Rightarrow is relation
 If sum is small \Rightarrow no relation

Work is done by Sheet Crunch

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Panel 4

Ex: Gender vs. Pres. Candidate in 2004

Contingency table results:

Rows: SEX
 Columns: WOULD HAVE VOTED FOR IN 2004

Cell format				
Count				
Expected count				
	Bush	Kerry	Nader	Total
Female	106 105.1	170 166.5	63 67.37	339
Male	89 89.9	139 142.5	62 57.63	290
Total	195	309	125	629

Chi-Square test:

Statistic	DF	Value	P-value
Chi-square	2	0.76769374	0.6745

If p-value of Chi-Square Test is

$p \geq 0.05 \Rightarrow$ no relation
 $p < 0.05 \Rightarrow$ is relation

Caution: This procedure (Chi-square test) may be invalid if any expected value is less than 5

↑
 $p = 0.6745 \Rightarrow$ No relation

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Panel 5

Contingency table results:

Rows: DEATH PENALTY FOR MURDER

Columns: LIBERAL OR CONSERVATIVE

Cell format								
Count								
Expected count								
	1 - extremely liberal	2 - liberal	3 - slightly liberal	4 - moderate	5 - slightly conservative	6 - conservative	7 - extremely conservative	Total
favor	28 45.06	105 151.8	126 143.8	468 453.9	181 189.6	253 205.4	53 44.4	1214
oppose	40 22.94	124 77.25	91 73.2	217 231.1	75 86.38	57 104.6	14 22.6	618
Total	68	229	217	685	256	310	67	1832

Chi-Square test:

Statistic	DF	Value	P-value
Chi-square	6	109.52265	<0.0001

all expected values ≥ 5 ✓

$p < 0.0001 \Rightarrow$ There is a relation between variables.

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Panel 6

Book goes to more detail into this question:

Lambda λ

Gamma γ values for more precise analysis.

StatCrunch does not compute those λ, γ values, so we'll skip them for now.

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Panel 7

Correlation for Numeric Variables

HS GPA	Colleg GPA
3.8	2.8
3.1	2.2
4.0	3.5
2.5	1.9
3.3	2.5

Q1: Are they related?
Q2: How strong is association?
Q3: Make predictions

Compute Correlation Coefficient r:

$$S_{xx} = \sum x^2 - \frac{(\sum x)^2}{n}$$

$$S_{yy} = \sum y^2 - \frac{(\sum y)^2}{n}$$

$$S_{xy} = \sum xy - \frac{(\sum x)(\sum y)}{n}$$

$$r = \frac{S_{xy}}{\sqrt{S_{xx} \cdot S_{yy}}}$$

Panel 8

x	y	x ²	y ²	xy
3.8	2.8	14.44	7.84	3.8 · 2.8 = 10.64
3.1	2.2	9.61	4.84	6.82
4.0	3.5	16.00	12.25	14.00
2.5	1.9	6.25	3.61	4.75
3.3	2.5	10.89	6.25	8.25
<u>16.7</u>	<u>12.9</u>	<u>52.19</u>	<u>34.79</u>	<u>44.46</u>

$$S_{xx} = \sum x^2 - \frac{(\sum x)^2}{n} = 52.19 - \frac{16.7^2}{5} = 1.412$$

$$S_{yy} = \sum y^2 - \frac{(\sum y)^2}{n} = 34.79 - \frac{12.9^2}{5} = 1.508$$

$$S_{xy} = \sum xy - \frac{(\sum x)(\sum y)}{n} = 44.46 - \frac{16.7 \cdot 12.9}{5} = 1.774$$

$$r = \frac{S_{xy}}{\sqrt{S_{xx} \cdot S_{yy}}} = \frac{1.774}{\sqrt{1.412 \cdot 1.508}} = 0.9416$$

x is independent var (HS)
y is the dependent var (College)

Panel 9

The Correlation Coefficient r :

- is always between -1 and 1
- if close to 1 or -1 , there is a strong relation between variables
if close to 0 , no relation
- if positive \Rightarrow positive relation (if x gets bigger, y gets bigger)
if negative \Rightarrow negative relation (if x gets bigger, y gets smaller)

In our example: $r = 0.9 \Rightarrow$ strong positive relation between X, Y ,

i.e. HS GPA (x) is a good predictor of College GPA (y)