

Panel 1

The Nyquist Theorem

≈ 1924 by Nyquist

Theorem: Assume a signal is filtered through a low-pass filter of H Hz, and the signal consists of V discrete levels. Then

$$\text{max data rate} = \boxed{2 \cdot H \log_2(V) \text{ bps (bits per sec)}}$$

Ex.: 3 KHz filter, binary signals

$$\Rightarrow 2 \cdot 3000 \cdot \log_2(2) = 6000 \text{ bps}$$

$$\text{Use 16 levels} \Rightarrow 2 \cdot 3000 \log_2(16) = 24000 \text{ bps}$$

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Panel 2

Nyquist-Shannon Theorem

Nyquist assume perfect channel, i.e. no noise

Nyquist-Shannon Theorem For a channel with bandwidth H and signal-to-noise ratio S/N

$$\Rightarrow \text{max. data rate} = \boxed{H \log_2(1 + S/N)}$$

Eng. measure S/N in dB

$$\text{dB} = 10 \log_{10}(S/N) \Rightarrow S/N = 10 \Rightarrow 10 \text{ dB}$$

100

$$S/N = 100 \Rightarrow 20 \text{ dB}$$

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Panel 3

Nyquist-Shannon : $\max \text{ bits/sec} = f \log_2 (1 + \frac{S}{N})$

Typical analog voice-grade telephone system has

3000 Hz bandwidth and signal-to-noise ratio of 30 dB

$$\Rightarrow 30 \text{ dB} = 10 \log_{10} (\frac{S}{N})$$

$$\Rightarrow \frac{S}{N} = 1000$$

$$\Rightarrow \max \text{ rate} = 3000 \log_2 (1001) = 3000 \cdot 10 = \underline{\underline{30000 \text{ bps}}}$$

$\swarrow = 1024$

regardless of anything!

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Panel 4

Transmission Media

Magnetic Tape:

8 mm tape \sim 7 GB data
 standard box = 1000 tapes } 7000 GB

Ship in 24 Hours via UPS

$$\Rightarrow 7000 \cdot 8 \text{ GB} / 24 \cdot 60 \cdot 60 \approx \underline{\underline{648 \text{ Gbps}}}$$

Compares well to 1 Gbps Ethernet!

Cost: 1000 tapes = \$5000, 10x reusable

$$\Rightarrow \$500 + \$200 \text{ shipping} = \$700$$

$$\Rightarrow \frac{700}{7000 \text{ GB}} = 10 \text{ cents per } \underline{\underline{GB}}$$

Panel 5

Twisted Pair:

Tapes have high bandwidth but poor delay characteristics

Twisted pair = 2 copper wires twisted

2 parallel wires = antenna

2 twisted wire = no antenna

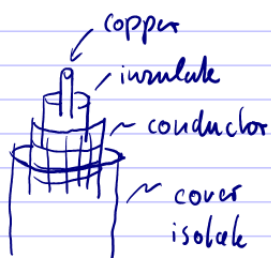
↙ reduce interference

Cat 3, Cat 5 cabling used by

Telephone and LAN

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Panel 6

Coaxial Cable

Broadband coax (50 ohm)

Broadband coax (75 ohm)

Broadband coax is used by TV cable system

up to 450 MHz ~ 100 km

TV channel uses 6 MHz (analog)

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Panel 7

Fiber Optics Cable

\approx 1000 km of fiber installed every day in US
 (100 km bundle with 10 strands = 1000 km)
 \approx 1970 computers (CDC) 1 instruct. per 100 μ sec
 \approx 1990 computer (Cray) 1 instr. per 1 μ sec
 \Rightarrow Factor 10 improvement per decade!

Data Comm.: 1970: 56 kbps (ARPANET)
 1990: 1 Gb
 \Rightarrow factor > 100 improvement per decade

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Panel 8

More on Fiber

CPU performance reaches physical limit
 Current fiber has bandwidth > 50 000 Gbps

Bottleneck (1Gb): optical/electric converters

Plus: Computers are slow, network rules
 Avoid computational overhead
 \Rightarrow waste bandwidth

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